They show bivariate data - two types of data Paired dater
Eg Doctor height and weight BMI
Scatter graph
The $x$ axis (hovizonta) represents one type of data The $y$ axis (vertical) represents the other type of data Eg1) A teacher recorded the no. of hours students spent studying and the marks they achieved out of 100 in a test.

| Hours spent | 3 | 5 | 2 | 6 | 7 | 1 | 2 | 7 | 1 | 7 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Test score | 80 | 90 | 75 | 80 | 90 | 50 | 65 | 85 | 40 | 100 |

Show this on a scatter plot


Correlation: describes the strength and direction of the unear relationship between the two types of data

The closer the scatter graph data is to a straight line, the stranger the correlation.
The correlation coefficient $r$ and this ranges from $-1 \leqslant r \leqslant 1 \quad\{r:-1,0,+1\}$ decimals between
'Ine correluicur cun.........
fram $-1 \leq r \leq 1$
decumals between -1 and +1
Scatter graphs and
correlation coefficient
(1)


Strong negatue


Weak negative corvelatian
(5)


Weak courelation positure

(2)

moderate correlation. negatue

no correlation


Moderate Positure corecelation


Strang positue courelation.

T\&T3 13.5
$\underset{\text { T\&T3 }}{\substack{\text { Tedf } \\ \text { 13.5.pptx } \\ \hline}}$

PROJEGT MATHS
Texit Tests
Leaving

Representing Data

Section 13.5 Scatter graphs

## Example 1

On a journey between two towns, Andrew wrote down the number of kilometres that were left on the journey. He did this every ten minutes.
The table below shows the data he recorded

| Time (mins) | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 | 100 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Kilometres to go | 72 | 60 | 50 | 42 | 40 | 32 | 25 | 18 | 10 | 0 |

Uraw a scatter grapn to illustrate
this data.

## Example 2

The table shows the weights and heights of 12 people.

| Height (cm) | 150 | 152 | 155 | 158 | 158 | 160 | 163 | 165 | 170 | 175 | 178 | 180 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Weight (kg) | 57 | 62 | 63 | 64 | 58 | 62 | 65 | 66 | 65 | 70 | 66 | 67 |

(i) Draw a scatter graph to show this data.
(ii) Describe the strength and type of correlation between these heights and weights.


## Exercise 13.5

1. Four scatter graphs are shown below.




(i) Which of these graphs shows the strongest positive correlation?
(ii) Which of these graphs shows negative correlation?
(iii) Which of these graphs shows the weakest correlation?

## Exercise 13.5

2. Here are sketches of six scatter graphs:






Which diagram(s) show
(i) positive correlation
(ii) negative correlation
(iii) no correlation
(iv) strong negative correlation?

Describe the correlation in graph F .

## Exercise 13.5

3. This scatter graph shows the number of books read by some children and the reading ages of these children.
(i) How many children have read more than 100 books?
(ii) One of these children has read 50 books. What is the reading age of this child?
(iii) Describe the relationship


## Exercise 13.5

4. The examination marks of a sample number of students in both their mock and final examinations are shown in the given scatter graph.
(i) Describe the correlation shown in the graph.
(ii) What can you say about the relationship between the mock and final marks of the students?


## Exercise 13.5

5. This scatter diagram shows the weights, in kg , and the heights, in cm , of 20 male members of a basketball club.

(i) Write down the weight of the heaviest member.
(ii) Write down the height of the shortest member.
(iii) One member is particularly heavy for his height Write down the height and weight of this member.
(iv) Describe the correlation shown in this graph.

## Exercise 13.5

6. Ten children are given two tests to complete. One test involves some number puzzles. The other test involves spotting mistakes in pictures.
The table shows the scores in the tests for these children.

| Child | A | B | C | D | E | F | G | H | I | J |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number puzzle score | 12 | 7 | 10 | 3 | 7 | 10 | 5 | 5 | 12 | 14 |
| Picture puzzle score | 3 | 12 | 7 | 16 | 10 | 5 | 14 | 12 | 5 | 1 |

(i) Draw a scatter graph to show this data.
(Put the number score on the horizontal axis.)
(ii) Describe the strength and type of correlation between these scores. Does the type of correlation surprise you? Explain.

## Exercise 13.5

7. Ben wants to buy a secondhand bike.

He records the age and price of the type he wants from a website.

| Age (years) | 6 | 3 | 2 | 4 | 6 | 1 | 4 | 8 | 2 | 7 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Price (€) | 60 | 180 | 240 | 120 | 100 | 280 | 160 | 40 | 200 | 50 |

(i) Draw a scatter graph of this information on graph paper, putting age on the horizontal axis.
(ii) What does the scatter graph tell you about the connection between the ages of these bikes and their prices?
(iii) Describe, in two words, the correlation that exists.

## Exercise 13.5

8. The table shows the marks of 15 students taking Paper 1 and Paper 2 of a maths exam. Both papers were marked out of 40 .

| Paper 1 | 36 | 34 | 23 | 24 | 30 | 40 | 25 | 35 | 20 | 15 | 35 | 34 | 23 | 35 | 27 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Paper 2 | 39 | 36 | 27 | 20 | 33 | 35 | 27 | 32 | 28 | 20 | 37 | 35 | 25 | 33 | 30 |

(i) Draw a scatter diagram to show this information.
(ii) Describe the correlation shown in the scatter diagram.

9. $\uparrow$





Four scatter graphs are shown above. For each of the following situations, choose the most appropriate of the scatter graphs. Explain your choice in each case.
(i) Boys' heights and their shoe sizes.
(ii) Men's weights and the times taken by them to complete a crossword puzzle.
(iii) Ages of cars and their selling prices.
(iv) Marks achieved in Maths Paper 1 and Maths Paper 2.

## Exercise 13.5

10. Describe the type of correlation you would expect between:
(i) the age of a boat and its secondhand selling price,
(ii) the heights of children and their ages,
(iii) the shoe sizes of children and the distances they travel to school,
(iv) time spent watching television and time spent studying,
(v) the number of cars on the road and the number of accidents.
11. (i) B
(ii) C
(iii) D
12. (i) $C$ and $F$
(ii) A and E
(iii) B and D
(iv) $A$; Perfect positive correlation
13. (i) $6 \quad$ (ii) 8.2 years
(iii) Weak positive
14. (i) Strong positive
(ii) Strong or close relationship
15. (i) $100 \mathrm{~kg} \quad$ (ii) 170 cm
(iii) $175 \mathrm{~cm}, 85 \mathrm{~kg}$ (iv) Weak positive
16. (ii) Strong negative correlation; Yes, as you
would expect positive correlation
17. (ii) Older bikes are cheaper
(iii) Strong negative
18. (ii) Strong positive correlation
19. (i) B
(ii) C
(iii) A
(iv) D
20. (i) Strong negative (ii) Strong positive
(iii) No correlation
(iv) Strong negative
(v) Strong positive
