

On the y axis  
x is ALWAYS 0  
 $x=0$

On the x axis  
y is ALWAYS 0  
 $y=0$

Eg 1 Graph the line  $2x+y=6$

you need to find where the line cut the y axis ( $x=0$ ) and x axis ( $y=0$ )

x axis  
 $y=0$  sub in 0 for y in the equation.

$$2x+(0)=6$$

$$2x=6$$

$$\div 2 \mid x=3 \mid \div 2$$

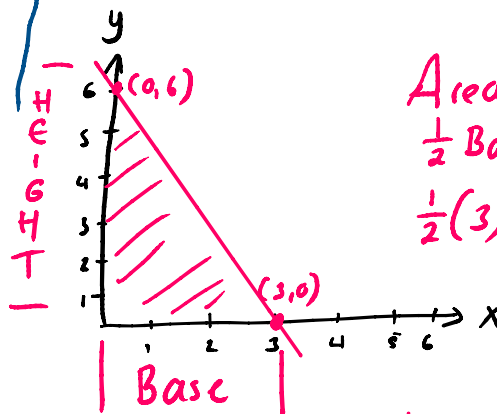
Point (3,0)

y axis  
 $x=0$  sub in 0 for x in the equation.

$$2(0)+y=6$$

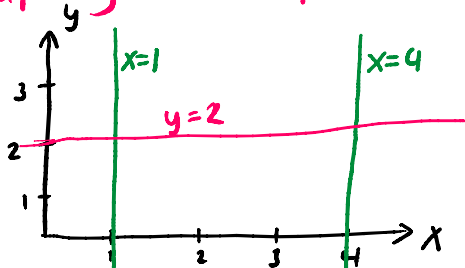
$$y=6$$

Point (0,6)



Area of the  $\Delta$   
 $\frac{1}{2}$  Base  $\times$   $\perp$  height  
 $\frac{1}{2}(3) \times 6 = 9 \text{ units}^2$

Graphing lines parallel to the axis



Lines // to the y axis  
 $x=a, a \in \mathbb{Z}$

Lines // to the x axis  
 $y=a, a \in \mathbb{Z}$

[1W  $\rightarrow$  H1W Pg 222 Pg 223  
Q1+2 Q4



chapter **11** **Coordinate Geometry –  
The Line**

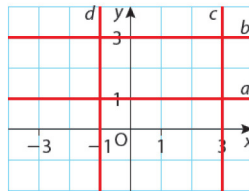
**Section 11.6 Graphing lines**

**Example 1**

If the point  $(k, 3)$  is on the line  $4x - 3y + 1 = 0$ , find the value of  $k$ .

### Exercise 11.6

1. Write down the equations of the lines  $a$ ,  $b$ ,  $c$  and  $d$  shown on the right.



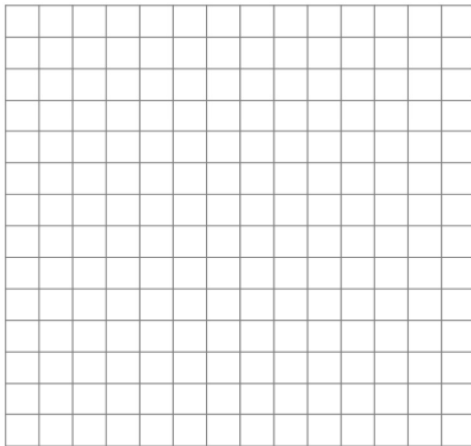
2. Draw a pair of axes and sketch these four lines:

(i)  $x = 4$

(ii)  $y = 2$

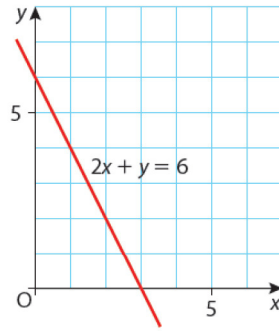
(iii)  $x = -2$

(iv)  $y = -3$



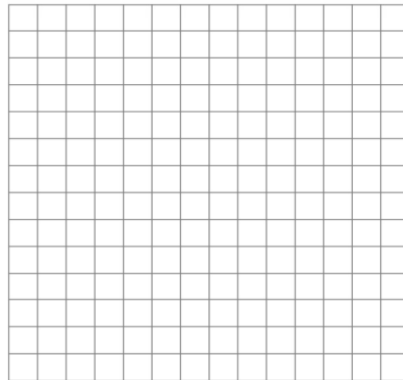
3. Use the graph of the line  $2x + y = 6$  to write down

- (i) the value of  $x$  when  $y = 0$
- (ii) the coordinates of the point where the line crosses the  $y$ -axis
- (iii) the value of  $y$  when  $x = 1$
- (iv) the value of  $x$  when  $y = 2$
- (v) the area of the triangle formed by the line, the  $x$ -axis and the  $y$ -axis.



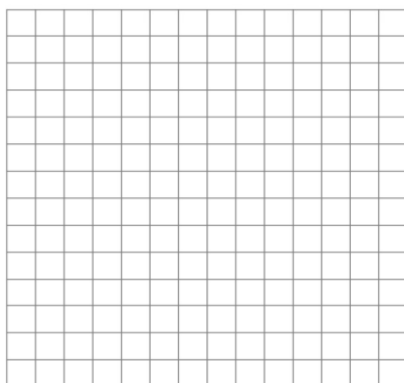
4. A straight line has equation  $x + y = 5$ .

- (i) By substituting  $x = 0$ , find the coordinates of the point where the line crosses the  $y$ -axis.
- (ii) By substituting  $y = 0$ , find the coordinates of the point where the line crosses the  $x$ -axis.
- (iii) Draw a graph of the line  $x + y = 5$ .



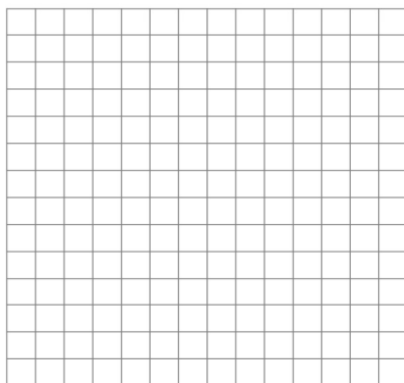
5. A straight line has equation  $3x + y = 6$ .

- (i) By substituting  $x = 0$ , find the coordinates of the point where the line crosses the  $y$ -axis.
- (ii) By substituting  $y = 0$ , find the coordinates of the point where the line crosses the  $x$ -axis.
- (iii) Draw a graph of the line  $3x + y = 6$ .



6. Find the coordinates of the points at which the line  $x - 2y - 6 = 0$  intersects the  $x$ -axis and  $y$ -axis.

Now use these points to draw a sketch of the line.



7. Find the coordinates of the points where the line  $x - 2y = 5$  intersects the  $x$ -axis and  $y$ -axis. Hence draw a sketch of the line.



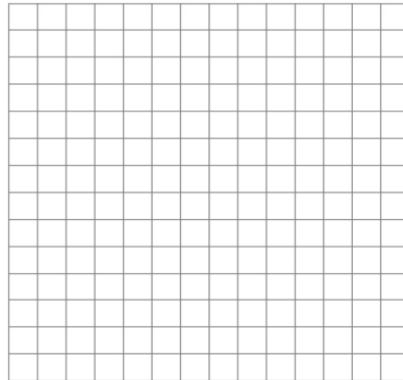
8. Draw these graphs on the same diagram.

(i)  $x + y = 2$

(ii)  $x + y = 3$

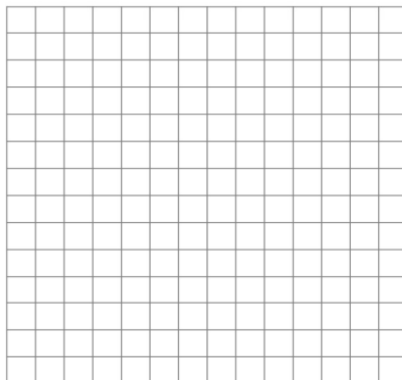
(iii)  $x + y = 5$

What do they all have in common?



9. Draw a sketch of the line  $2x - y + 6 = 0$ .

Hence write down the area of the triangle formed by the x-axis, the y-axis and the line.



10. The equations of the lines  $a$  and  $b$  are:

$$a: y = \frac{2}{3}x + 2$$

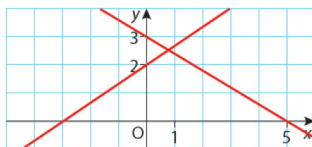
$$b: 3x + 5y - 15 = 0$$

(i) Which line intersects the y-axis at  $(0, 2)$ ?

(ii) Which line intersects the x-axis at  $(5, 0)$ ?

(iii) Use the slopes of the two lines to investigate whether the lines are perpendicular to each other.

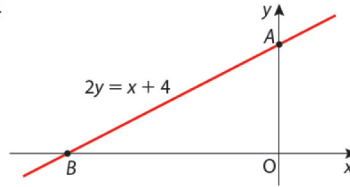
(iv) Write down the area of the triangle formed by the line  $3x + 5y - 15 = 0$ , the x-axis and the y-axis.



11. The diagram shows a sketch of the line  $2y = x + 4$

- (i) Find the coordinates of points  $A$  and  $B$ .
- (ii) What is the gradient of the line?

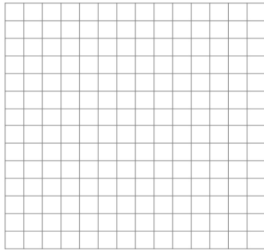
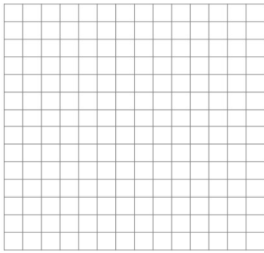
Gradient is another word for slope.



12. Each of the following lines contains the origin  $(0, 0)$ .

By taking a value for  $x$  and then finding the corresponding  $y$ -value, sketch each of the lines on separate diagrams:

- (i)  $x - 2y = 0$
- (ii)  $x + 3y = 0$
- (iii)  $3x - y = 0$
- (iv)  $x - 4y = 0$

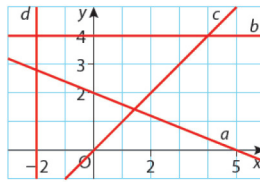




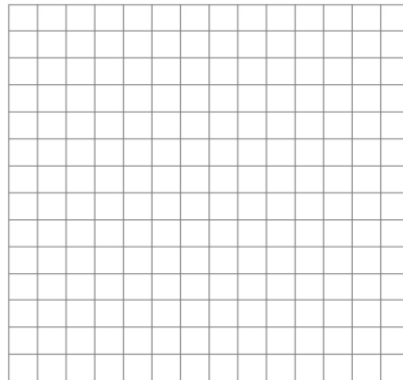
13. The lines  $a$ ,  $b$ ,  $c$  and  $d$  are graphed in the given diagram.

Match each line with one of these equations:

- (i)  $x = -2$
- (ii)  $x - y = 0$
- (iii)  $2x + 5y = 10$
- (iv)  $y = 4$



14. (i) Verify that  $(2, -5)$  is on the line  $2x + y + 1 = 0$ .  
(ii) Verify that  $(2, -3)$  is on the line  $y = x - 5$ .  
(iii) Show that  $(-3, 1)$  is not on the line  $x - 3y + 1 = 0$ .  
(iv) Investigate if  $(2, 0)$  is on the line  $2x - y + 3 = 0$ .



**15.** Show that  $(-3, 1)$  is on the line  $2x + 4y + 2 = 0$ .

**16.** If  $(1, 4)$  is on the line  $2x + y + k = 0$ , find the value of  $k$ .

**17.** If  $(2, -3)$  is on the line  $x + ky + 7 = 0$ , find the value of  $k$ .

- 18.** (i) Find the value of  $k$  if the line  $2x + ky - 8 = 0$  contains the point  $(3, 1)$ .  
(ii) If  $(1, t)$  lies on the line  $y = 2x + 3$ , find the value of  $t$ .

## Answers

### Exercise 11.6

1.  $a: y = 1, b: y = 3, c: x = 3, d: x = -1$
3. (i) 3                      (ii) (0, 6)              (iii) 4  
(iv) 2                      (v) 9 sq. units
4. (i) (0, 5)                      (ii) (5, 0)
5. (i) (0, 6)                      (ii) (2, 0)
6. (6, 0), (0, -3)
7. (5, 0), (0,  $-2\frac{1}{2}$ )
8. Same slope, i.e. all parallel to each other
9. 9 sq. units

## Answers

10. (i)  $a$                       (ii)  $b$   
(iii) Not perpendicular (iv)  $\frac{15}{2}$  sq. units
11. (i) A(0, 2), B(-4, 0)      (ii)  $\frac{1}{2}$
13. (i)  $d$               (ii)  $c$               (iii)  $a$               (iv)  $b$
14. (iv) Not on this line
16. -6
17. 3
18. (i) 2                      (ii) 5