

Factorize Fractions

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Eg1 $\frac{\cancel{15}^3}{\cancel{10}^2} \quad \text{HCF} = 5 \quad \text{Ans} \quad \frac{3}{2}$

Eg2 $\frac{\cancel{7}^1 x}{\cancel{35}^5} \quad \text{HCF} = 7 \quad \text{Ans} = \frac{1x}{5} \text{ OR } \frac{x}{5}$

Eg3 $\frac{\cancel{9}^{3x} x^2}{\cancel{3x}^1} \quad \text{HCF} = 3x \quad \text{Ans} = \frac{3x}{1} = 3x$

Eg4) $\frac{4a-8b}{3(a-2b)} = \text{HCF is } 4 = \frac{4(\cancel{a-2b})}{3(\cancel{a-2b})} = \frac{4}{3}$

Class work pg 29 Q 1+Q2.



T&T2 2.5
Simplifying...

Factors

chapter

2

29

Section 2.5 Using factors to simplify algebraic fractions

Example 1

Simplify

(i) $\frac{3n - 12}{n - 4}$

(ii) $\frac{3x^2 - 5x - 2}{x - 2}$

Exercise 2.5

1. Simplify each of the following:

(i) $\frac{14}{35}$

HCF
7

$$\frac{2}{5}$$

(ii) $\frac{7x}{14}$

HCF
7

$$\frac{1x}{2}$$

(iii) $\frac{9x^2}{3x}$

(iv) $\frac{8p^2}{2p}$

HCF
2p

$$\frac{4p}{1} = 4p$$

(v) $\frac{9x^2y}{3xy}$

HCF
3xy

$$\frac{3x}{1} = 3x$$

2. Simplify each of the following:

(i) $\frac{4x + 4y}{4}$

OR $\frac{1x+1y}{x+y}$

HCF
4

(ii) $\frac{12(a+b)}{3(a+b)}$

$\frac{12}{3} = 4$

(iii) $\frac{3x + 12}{x(x + 4)}$

$\frac{3(x+4)}{x(x+4)}$

$= \frac{3}{x}$

(iv) $\frac{4a - 8b}{3(a - 2b)}$

Simplify each of the following, using factors where necessary:

3. $\frac{(x-1)(x+3)}{x+3}$

$(x-1)$

4. $\frac{2(y-1)(y+3)}{y-1}$

$= 2(y+3)$

5. $\frac{x^2 + 8x + 7}{x+1}$ Quadratic

$(x+7)(x+1)$
 $\begin{array}{r} x^2 \quad 7 \\ \diagdown \quad \diagup \\ x \quad x \quad 7 \quad 1 \end{array}$
 $\begin{array}{r} + 1x \\ + 7x \\ \hline + 8x \end{array}$

$\frac{(x+7)(x+1)}{x+1} = x+7$

Simplify each of the following, using factors where necessary:

6. $\frac{x-4}{x^2-6x+8} = \frac{1}{x-2}$

$(x-4)(x-2)$

$(x-4)(x-2)$

$\begin{array}{r} x^2 \quad +8 \quad -2x \\ x \quad \quad 4 \quad 2 \\ \hline -4x \end{array}$

7. $\frac{x-2}{x^2+5x-14} = \frac{1}{x+7}$

$(x+7)(x-2)$

$\begin{array}{r} x^2 \quad -14 \quad -2x \\ x \quad \quad 7 \quad 2 \\ \hline +7x \end{array}$

8. $\frac{3x-3}{x^2-2x+1} = \frac{3(x-1)}{(x-1)(x-1)} = \frac{3}{x-1}$

HCF

$(x-1)(x-1)$

$\begin{array}{r} x^2 \quad \quad 1 \quad -1x \\ x \quad \quad 1 \quad -1x \\ \hline -2x \end{array}$

Class work
Pg 29 Q 9-19

Simplify each of the following, using factors where necessary:

9. $\frac{2x-6}{x^2+x-12} = \frac{2(x-3)}{(x+4)(x-3)} = \frac{2}{x+4}$

Ans = $\frac{2}{x+4}$

$\begin{array}{r} x^2 \quad 12 \quad -3x \\ x \quad \quad 4 \quad 3 \\ \hline +1x \end{array}$

10. $\frac{x^2+x-30}{x-5} = \frac{(x+6)(x-5)}{x-5} = x+6$

Ans = $x+6$

$\begin{array}{r} x^2 \quad 30 \quad -5x \\ x \quad \quad 6 \quad 5 \\ \hline +6x \end{array}$

11. $\frac{a^2+2ab}{3a+6b} = \frac{a(a+2b)}{3(a+2b)} = \frac{a}{3}$

Ans = $\frac{a}{3}$

- Test topics
- ① Algebra multiplication
 - ② Grouping
 - ③ DOTS
 - ④ Quadratic factorizing
 - ⑤ Substitution
 - ⑥ Factorize fractions
 - ⑦ Double inequality - number line
- Revision
Pg 30
Test yourself
Q1→5.

Simplify each of the following, using factors where necessary:

12. $\frac{x^2 - 9}{x - 3}$

13. $\frac{a^2 - 16}{3a - 12}$

14. $\frac{n + 9}{n^2 + 18n + 81}$

Simplify each of the following, using factors where necessary:

15. $\frac{4x - 8}{x^2 - 4}$

16. $\frac{2x^2 + 5x - 3}{2x - 1}$

17. $\frac{2x^2 + 11x + 15}{2x + 5}$

Simplify each of the following, using factors where necessary:

18. $\frac{ab - ac}{b - c}$

19. $\frac{5 - x}{x - 5}$

20. $\frac{3a + 9}{a^2 - 1} \div \frac{a + 3}{a - 1}$

Answers

Exercise 2.5

1. (i) $\frac{2}{5}$ (ii) $\frac{x}{2}$ (iii) $3x$ (iv) $4p$ (v) $3x$
2. (i) $x + y$ (ii) 4 (iii) $\frac{3}{x}$ (iv) $\frac{4}{3}$
3. $x - 1$ 4. $2(y + 3)$ 5. $x + 7$
6. $\frac{1}{x - 2}$ 7. $\frac{1}{x + 7}$ 8. $\frac{3}{x - 1}$
9. $\frac{2}{x + 4}$ 10. $x + 6$ 11. $\frac{a}{3}$
12. $x + 3$ 13. $\frac{a + 4}{3}$ 14. $\frac{1}{n + 9}$
15. $\frac{4}{x + 2}$ 16. $x + 3$ 17. $x + 3$
18. a 19. -1 20. $\frac{3}{a + 1}$